

Observer design and fault detection of Boolean control networks

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Introduction

Boolean control networks (BCN):

$$\left\{ \begin{array}{l} X_1(k+1) = f_1(X_1(k), \dots, X_n(k), U_1(k), \dots, U_m(k)) \\ \vdots \\ X_n(k+1) = f_n(X_1(k), \dots, X_n(k), U_1(k), \dots, U_m(k)) \\ Y_1(k) = h_1(X_1(k), \dots, X_n(k)) \\ \vdots \\ Y_p(k) = h_p(X_1(k), \dots, X_n(k)) \end{array} \right.$$

$X_1(k), \dots, X_n(k)$: States
 $U_1(k), \dots, U_m(k)$: Control inputs
 $Y_1(k), \dots, Y_p(k)$: Measured outputs
 $f_1(k), \dots, f_n(k), h_1(k), \dots, h_p(k)$: Boolean functions

} Binary signals (0/1)

Matrix expression of Boolean control networks

$$\begin{aligned}x(t+1) &= L \ltimes x(t) \ltimes u(t) \\ y(t) &= H \ltimes x(t)\end{aligned}$$

L, H : constant matrices (contain all information about Boolean functions)

$$x(t) \in \Delta_{2^n}, u(t) \in \Delta_{2^m}, y(t) \in \Delta_{2^p}$$

$$\Delta_{2^n} = \left\{ \underbrace{\begin{bmatrix} 1 \\ 0 \\ 0 \\ \vdots \\ 0 \end{bmatrix}}_{1 \times 2^n}, \begin{bmatrix} 0 \\ 1 \\ 0 \\ \vdots \\ 0 \end{bmatrix}, \dots, \begin{bmatrix} 0 \\ 0 \\ 0 \\ \vdots \\ 1 \end{bmatrix} \right\} = \{ \delta_{2^n}^1, \delta_{2^n}^2, \dots, \delta_{2^n}^{2^n} \}$$

Motivation

- Our work is motivated by one course “logic control systems” with focus on automaton and Petri nets. **Graphical tool → analytical approach?**
- The **semi-tensor product (STP)** introduced by Cheng and Co-workers provides a powerful and convenient tool for the analysis and design of BCN.
- **Key idea:** Matrix and vector expression of logical operation and logical variables through STP
- **Focus of this talk:** **Observer design** and **fault detection** for Boolean control networks

Main content

- Not all state variables can be measured → extension of the idea of Kalman filter to **observer design** for BCN
- Handling of unknown disturbances → Design of **unknown input observer**
- How to handle large-scale BCN? → **Distributed observer** design
- How to reduce computational efforts? → **Reduced-order observer**
- How to apply observer for fault detection purpose? → **observer-based fault detection for BCN and probabilistic BCN**
- Design control input signal to improve fault detection performance? → **observer-based active fault detection**

Main content in this talk

- Not all state variables can be measured → extension of the idea of Kalman filter to **observer design** for BCN
- Handling of unknown disturbances → Design of **unknown input observer**
- How to handle large-scale BCN? → **Distributed observer** design
- How to reduce computational efforts? → **Reduced-order observer**
- How to apply observer for fault detection purpose? → **observer-based fault detection for BCN** and **probabilistic BCN**
- Design control input signal to improve fault detection performance? → **observer-based active fault detection**

Especially related STP properties

Properties (Cheng et al., World Scientific, 2012)

- $(A \ltimes B)^T = B^T \ltimes A^T$
- Power-reducing matrix: $\Phi_n = [\delta_{2^n}^1 \otimes \delta_{2^n}^1 \quad \delta_{2^n}^2 \otimes \delta_{2^n}^2 \quad \cdots \quad \delta_{2^n}^{2^n} \otimes \delta_{2^n}^{2^n}]$:

$$X \ltimes X = \Phi_n \ltimes X$$

- $X \ltimes A = (I_{2^n} \otimes A) \ltimes X$
- Swap matrix $W_{[2^m, 2^n]}$: $X \ltimes Y = W_{[2^m, 2^n]} \ltimes Y \ltimes X$

Lemma 1

The element-wise multiplication of vectors $X \in \mathbb{R}^{2^n \times 1}$ and $Y \in \mathbb{R}^{2^n \times 1}$ can be described by using power-reducing matrix Φ_n :

$$X \odot Y = \Phi_n^T \ltimes X \ltimes Y, \text{ with } \Phi_n = [\delta_{2^n}^1 \otimes \delta_{2^n}^1 \quad \delta_{2^n}^2 \otimes \delta_{2^n}^2 \quad \cdots \quad \delta_{2^n}^{2^n} \otimes \delta_{2^n}^{2^n}]$$

Observer design

BCN:

$$\begin{aligned} x(t+1) &= L \ltimes x(t) \ltimes u(t) \\ y(t) &= H \ltimes x(t) \end{aligned}$$

Main purpose of observer design:

Get a good estimate $\hat{x}(t)$ based on the available information of $u(t)$ and $y(t)$.

Observer design for Boolean control networks (Zhang et al., CDC 2016)

$$\hat{x}(0) = H^T y(0)$$

$$\hat{x}(t) = \underbrace{L\hat{x}(t-1)u(t-1)}_{\text{Propogation of state estimate } \hat{x}(t-1)} \underbrace{\odot}_{\text{elementweis multiplication}} \underbrace{H^T y(t)}_{\text{Estimation of } x(t) \text{ directly from } y(t)}$$

$$= \Phi_n^T L \hat{x}(t-1) u(t-1) H^T y(t)$$

$$= \Phi_n^T (I_{2^n} \otimes H^T) L \hat{x}(t-1) u(t-1) y(t)$$

Example

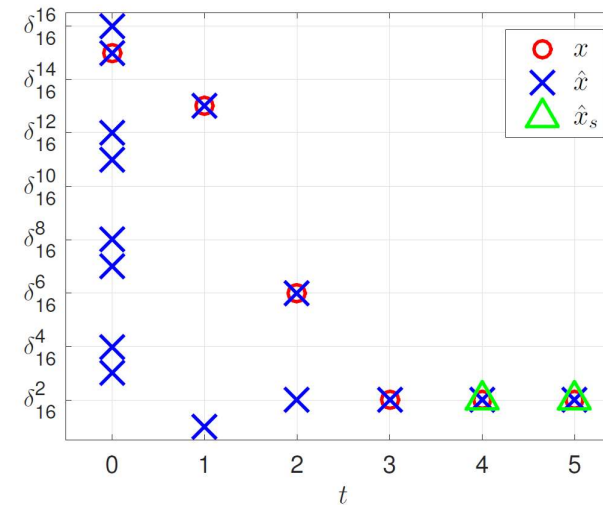
BCN:

$$\begin{cases} x_1(t+1) &= x_1(t) \vee x_3(t) \\ x_2(t+1) &= x_1(t) \\ x_3(t+1) &= u(t) \vee x_2(t) \vee x_4(t) \\ x_4(t+1) &= \neg x_3(t) \\ y(t) &= x_3(t) \end{cases}$$

**Input and output sequence
(logic value):**

t	0	1	2	3	4	5
u	0	1	1	0	0	
y	0	1	1	1	1	1

State estimate:



x : true state

$\hat{x}$: Luenberger-observer

$\hat{x}_s$: Shift-register observer

Unknown input observer design

Consider a BCN with unknown inputs

$$x(t+1) = Lx(t)u(t)d(t)$$

$$y(t) = Hx(t)$$

$u(t)$: control inputs

$d(t)$: unknown inputs



The BCN is said to be **unknown input reconstructible**, if for any possible input $d(t)$ a non-negative integer r can be found, so that with the knowledge of every admissible control input and output trajectory $\{u(0), y(0), u(1), y(1), \dots, u(t), y(t)\}, t \geq r$, the final state $x(t)$ can be unique determined.

Unknown input observer design

The set of states that can be reached at time $t + 1$ from a given state $x(t)$:

$$\begin{aligned}
 x(t+1) &= Lx(t)u(t)d(t) \\
 &= LW_{[2^{m_d}, 2^{n+m}]} d(t)x(t)u(t) \\
 &= LW_{[2^{m_d}, 2^{n+m}]} \left(\begin{bmatrix} 1 \\ 0 \\ \vdots \\ 0 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \\ \vdots \\ 0 \end{bmatrix} + \dots + \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 1 \end{bmatrix} \right) x(t)u(t) \\
 &= LW_{[2^{m_d}, 2^{n+m}]} \underbrace{\begin{bmatrix} 1 \\ 1 \\ \vdots \\ 1 \end{bmatrix}}_{\mathbf{1}_{2^{m_d}}} x(t)u(t) \\
 &= \tilde{L}x(t)u(t)
 \end{aligned}$$

Unknown input observer design

Introduce an **auxiliary system**

$$\begin{aligned}x(t+1) &= \tilde{L}x(t)u(t) \\ y(t) &= Hx(t)\end{aligned}$$

The state candidates in $\hat{x}(t)$ that can generate the output $y(t)$ are

$$\hat{x}(0) = H^T y(0)$$

$$\begin{aligned}\hat{x}(t) &= \tilde{L}\hat{x}(t)u(t) \odot H^T y(t) \\ &= \Phi_n^T \tilde{L}\hat{x}(t-1)u(t-1)H^T y(t) \\ &= \Phi_n^T (I_{2^n} \otimes H^T) \tilde{L}\hat{x}(t-1)u(t-1)y(t)\end{aligned}$$

Unknown input observer design

Theorem for checking Unknown Input Reconstructibility

The BCN is unknown input reconstructible, if and only if the following two conditions are satisfied:

- (1) The matrix $\Phi_n^T(I_{2^n} \otimes H^T)\tilde{L}$ contains only zero columns or columns with only one non-zero entry.
- (2) The auxiliary system is reconstructible.

Example

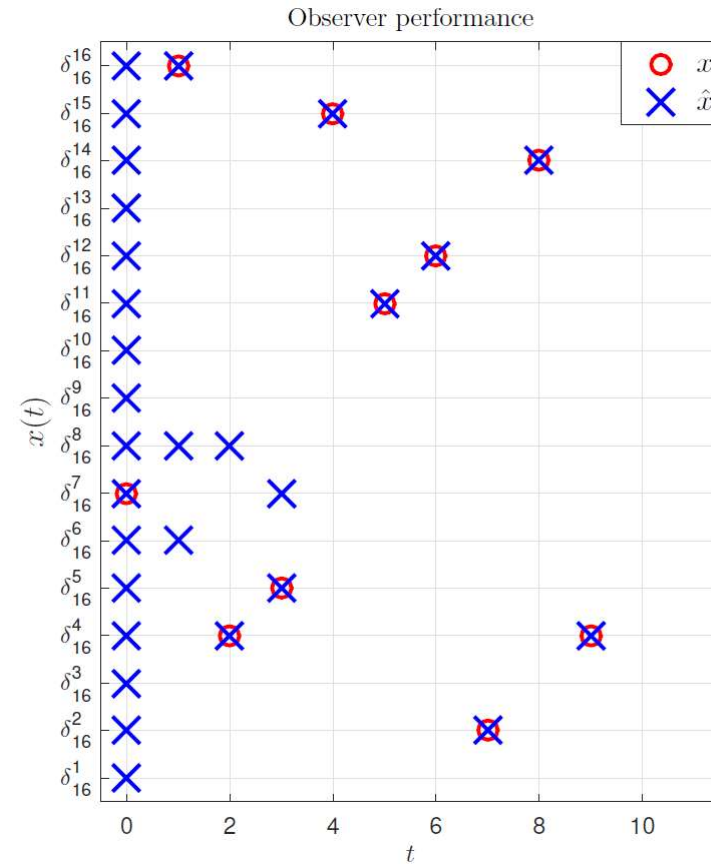
BCN with unknown inputs ξ and ω :

$$\begin{cases} x_1(t+1) = u(t) \wedge \neg x_6(t) \\ x_2(t+1) = \neg x_1(t) \\ x_3(t+1) = \neg x_1(t) \wedge (x_5(t) \vee x_3(t)) \\ x_4(t+1) = x_2(t) \wedge \neg x_6(t) \\ x_5(t+1) = (x_4(t) \vee \neg x_3(t)) \wedge \xi(t) \\ x_6(t+1) = x_5(t) \wedge (\neg x_6(t) \vee \neg x_2(t)) \\ y_1(t) = x_2(t) \vee \omega(t) \\ y_2(t) = x_3(t), y_3(t) = x_5(t) \end{cases}$$

**Input and output sequence
(logic value):**

t	0	1	2	3	4	5	6	7	8	9
u	1	1	1	1	1	0	1	0	1	
ξ	1	1	1	1	0	1	1	0	1	
ω	1	1	0	0	0	0	0	0	0	0
y_1	1	1	1	0	0	1	1	1	0	1
y_2	1	0	0	0	0	1	1	1	0	0
y_3	0	0	1	1	1	0	0	0	0	1

State estimate:



x : true state ($x_1x_2x_4x_6$)

$\hat{x}$: unknown input observer

Observer design for large-scale BCN

Main Challenges:

- High dimensional matrices L and H
- difficulty in the implementation of the observer due to memory and computational efforts

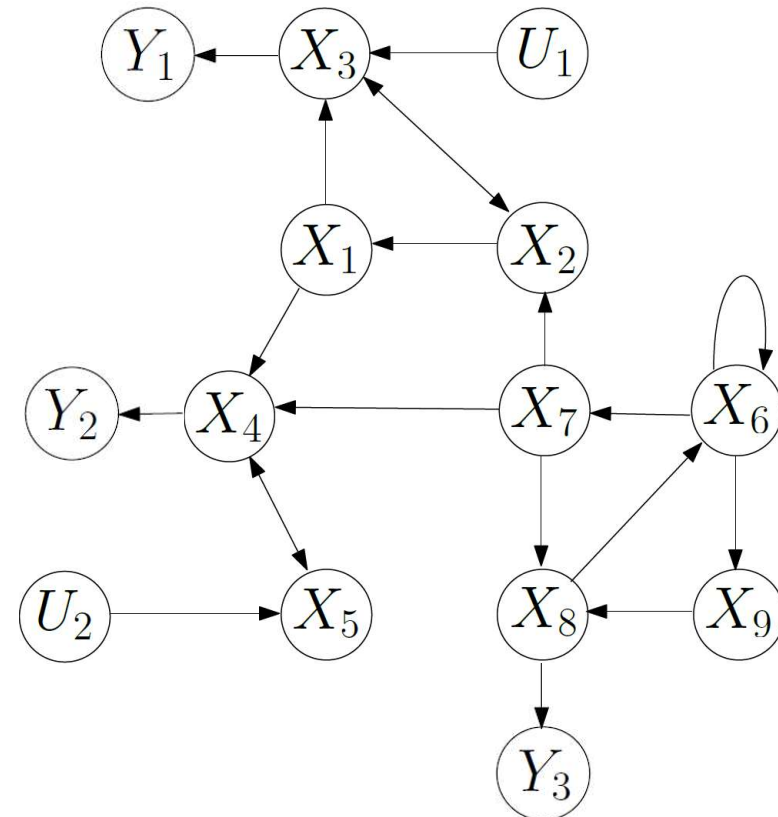


Distributed observer design

Basic idea of distributed observer design

Step 1: Express the large-scale Boolean network as a directed graph

$$\left\{ \begin{array}{l} X_1(t+1) = X_2(t) \\ X_2(t+1) = X_3(t) \wedge X_7(t) \\ X_3(t+1) = X_1(t) \wedge X_2(t) \wedge U_1(t) \\ X_4(t+1) = \neg X_1(t) \wedge X_5(t) \wedge X_7(t) \\ X_5(t+1) = X_4(t) \wedge U_2(t) \\ X_6(t+1) = X_6(t) \vee X_8(t) \\ X_7(t+1) = X_6(t) \\ X_8(t+1) = X_5(t) \vee X_7(t) \vee X_9(t) \\ X_9(t+1) = \neg X_8(t) \\ Y_1(t) = X_3(t), \quad Y_2(t) = X_4(t), \quad Y_3(t) = X_8(t) \end{array} \right.$$



Basic idea of distributed observer design

Step 2: Partition the large-scale boolean networks into subnetworks

$$\mathcal{X} = \mathcal{X}_1 \cup \mathcal{X}_2 \cup \dots \cup \mathcal{X}_\alpha,$$

$$\mathcal{U} = \mathcal{U}_1 \cup \mathcal{U}_2 \cup \dots \cup \mathcal{U}_\alpha,$$

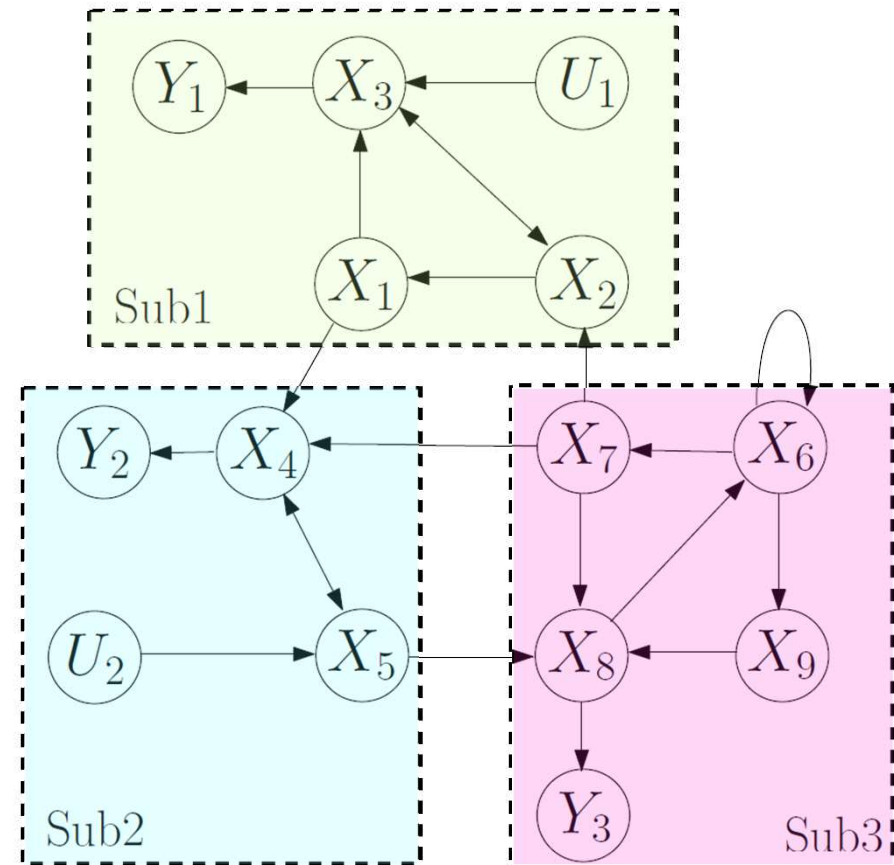
$$\mathcal{Y} = \mathcal{Y}_1 \cup \mathcal{Y}_2 \cup \dots \cup \mathcal{Y}_\alpha,$$

i -th subnetwork:

$$\mathcal{N}_i = \mathcal{X}_i \cup \mathcal{U}_i \cup \mathcal{Y}_i$$

In-neighbors to the i -th subnetwork: the incoming edges from other subnetworks.

Each state and output belongs to only one subnetwork.

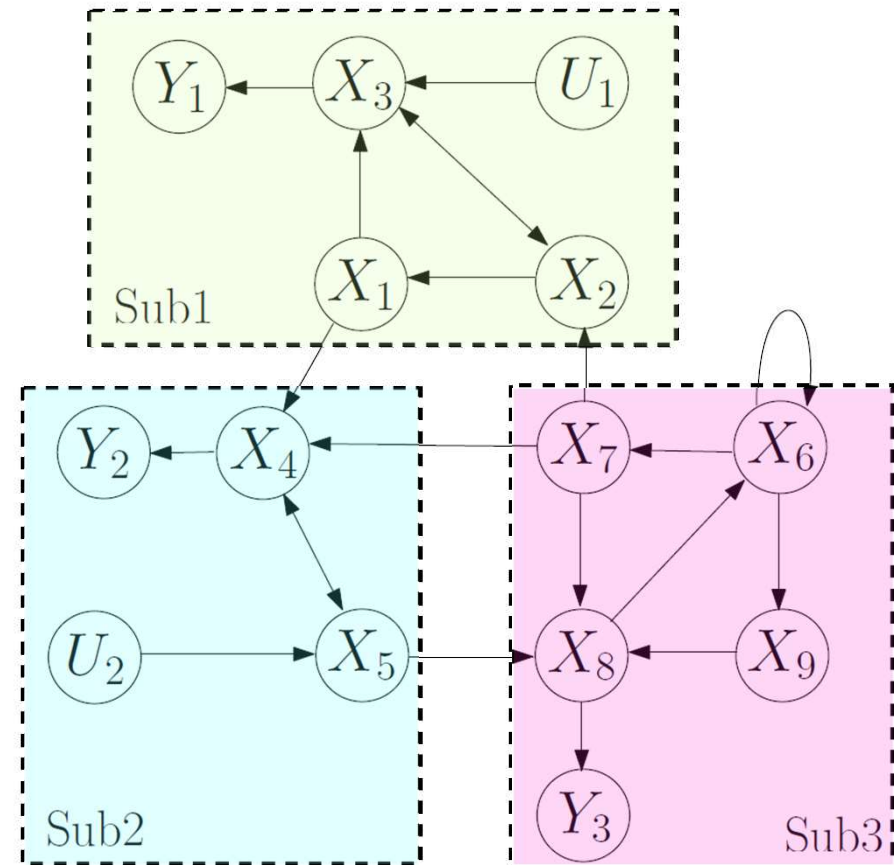


Basic idea of distributed observer design

Step 2: Partition the large-scale boolean networks into subnetworks

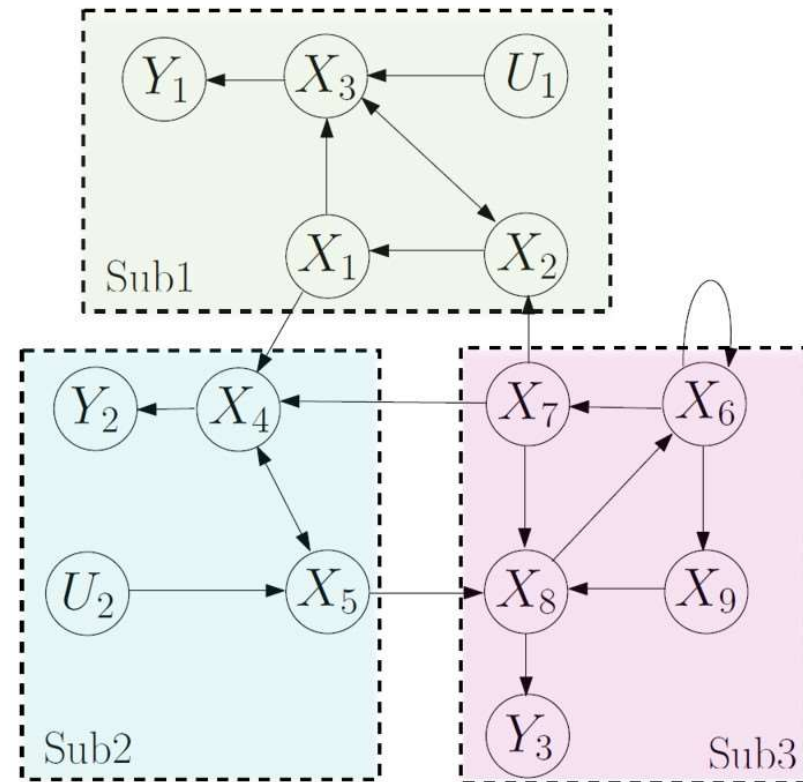
Basic requirement on partition:

- Each subnetwork should contain a small number of states $\rightarrow$ reduce memory and computational efforts
- Each subnetwork should connect to a small number of in-neighbors subsystems $\rightarrow$ reduce communication



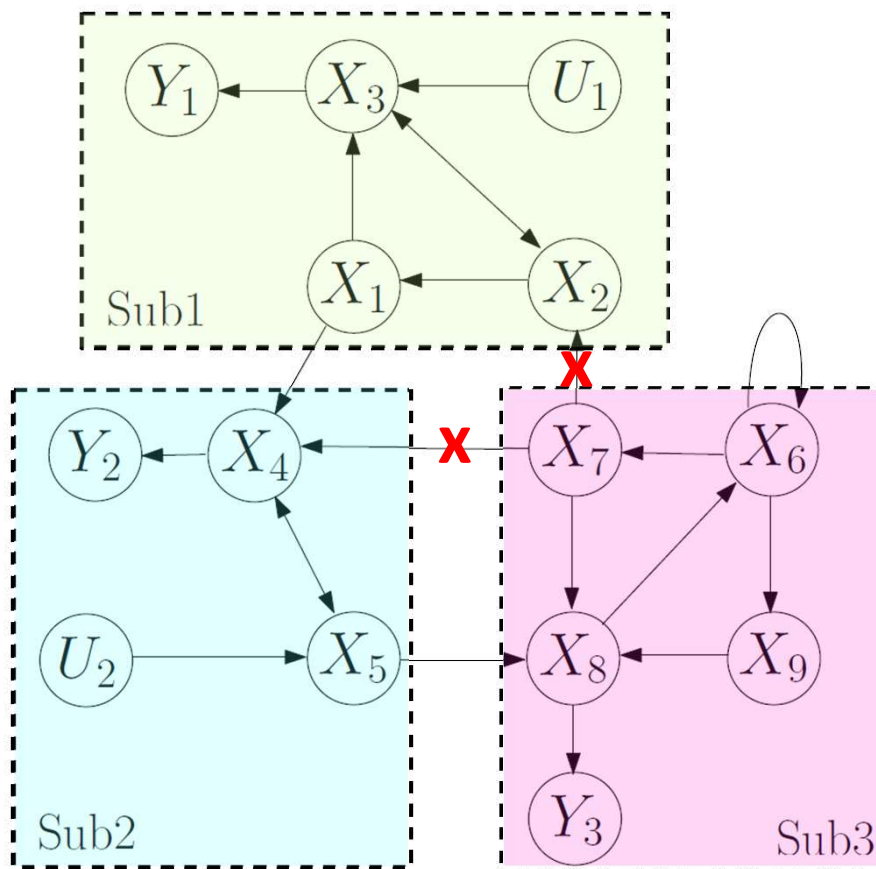
Basic idea of distributed observer design

Step 3: For each subnetwork, design a local observer to estimate the states. Aggregate the results to get the estimate of all states.



Distributed observer design

Consider at first a simple case:

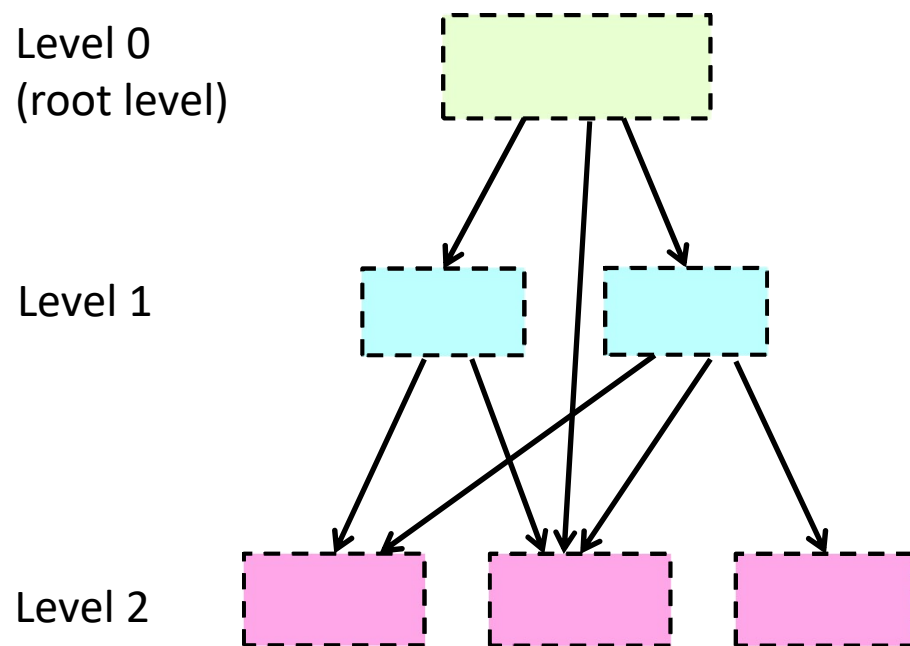


Estimation procedure:

- Estimate the states of Subnetwork 1 (who has no in-neighbors)
- Estimate the states of the Subnetwork 2
- Estimate the states of the Subnetwork 3

Distributed observer design

Large-scale BCN with acyclic structure: No directed cycles exists in the graph

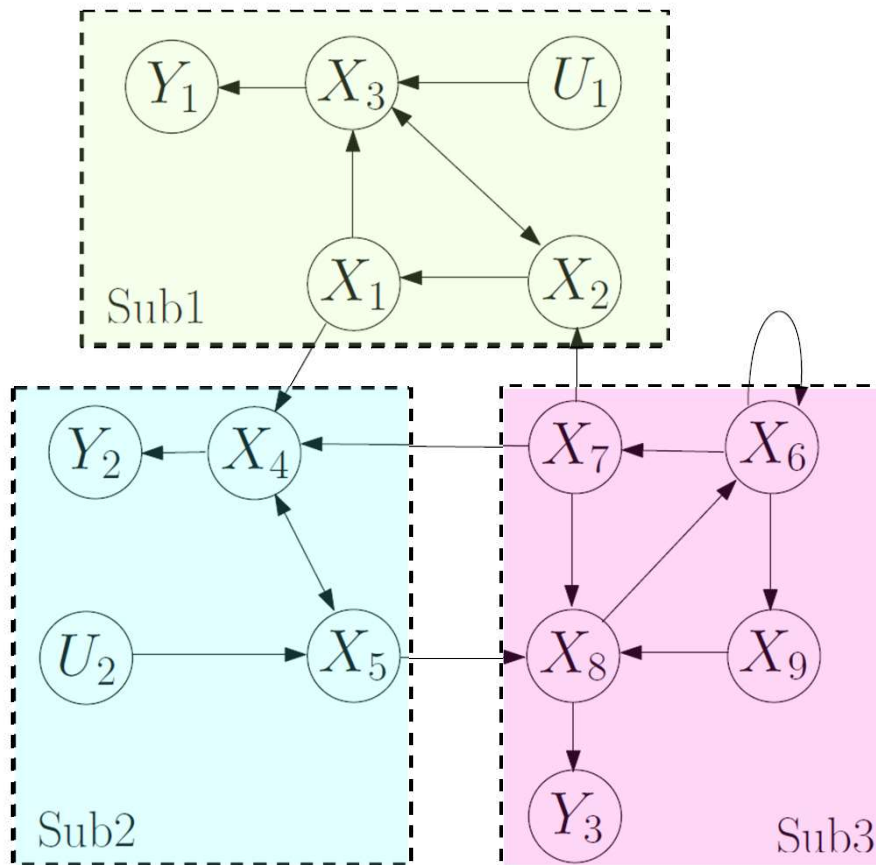


- Sort the subnetworks into β levels.
- A large-scale BCN with acyclic structure is reconstructible, if all subnetworks are reconstructible.
- The minimal reconstructibility index of the whole network can be estimated based on the minimal reconstructibility index of subnetworks.

How to handle large-scale BCNs which don't have acyclic structure?

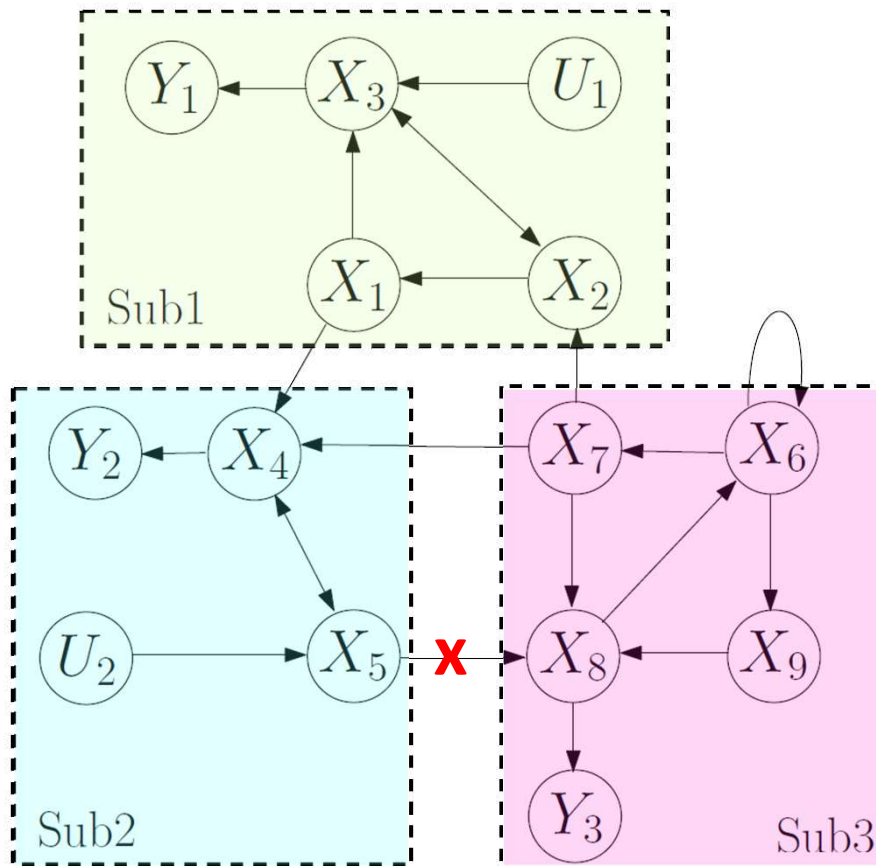
Distributed observer design

Consider our example before:



- (1) Subsystem 1, 2, 3 are reconstructible.
- (2) Subsystem 3 is unknown input reconstructible with respect to the incoming-Edge from X_5 . → The incoming-edge from X_5 to X_8 can be cut off.

Example



- (1) Subsystem 1, 2, 3 are reconstructible.
- (2) Subsystem 3 is unknown input reconstructible with respect to the incoming-Edge from X_5 . $\rightarrow$ The incoming-edge from X_5 to X_8 can be cut off.
- (3) Cutting off the incoming edge from X_5 to X_8 results in a directed acyclic graph.

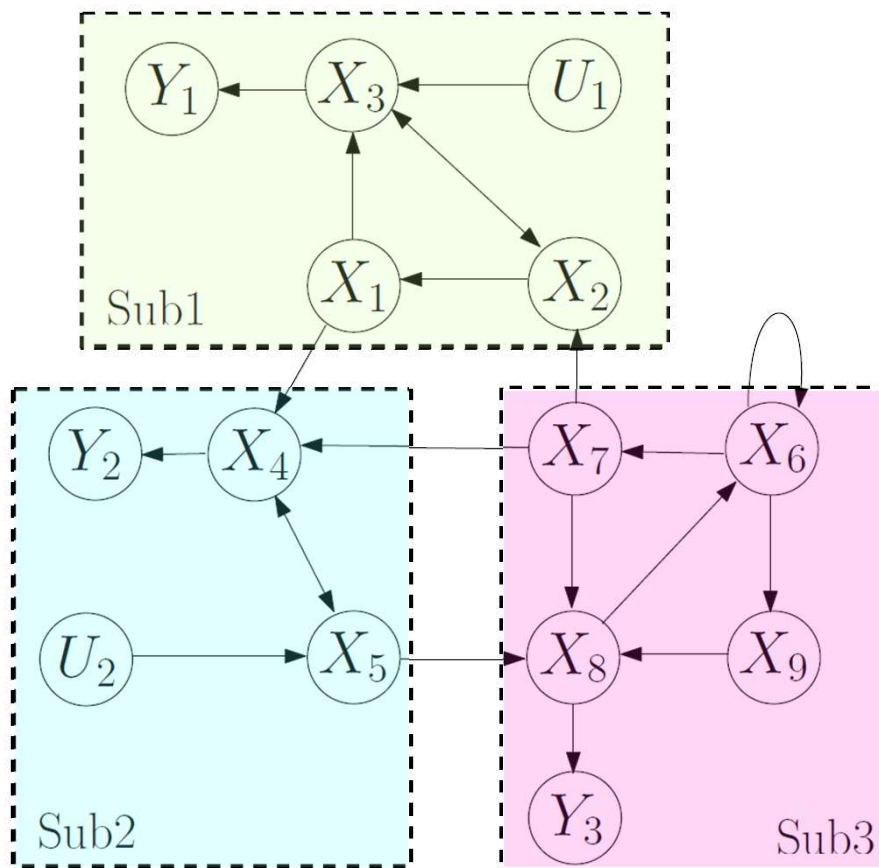
Level 0: Sub3

Level 1: Sub 1

Level 2: Sub2

Distributed observer design

Large-scale BCN with arbitrary structure



A large-scale BCN is reconstructible, if

- (1) All subnetworks are reconstructible.
- (2) There exist a set Ψ of subnetworks, which are unknown input reconstructible with respect to the states from their in-neighbors.
- (3) Cutting off the incoming edges of all subnetworks in the set Ψ results in a directed acyclic graph.

Distributed observer design

Design procedure:

Step 1: After the partition of the large-scale BCN, we get a set of subnetworks

$$\begin{aligned}x_i(t+1) &= L_i x_i(t) u_i(t) z_i(t) \\ y_i(t) &= H_i x_i(t), \quad i = 1, \dots, \alpha\end{aligned}$$

$z_i(t)$: the coupling states from the in-neighbors of the i -th subnetwork

Step 2: Check the reconstructibility and the unknown input reconstructibility of each subnetwork

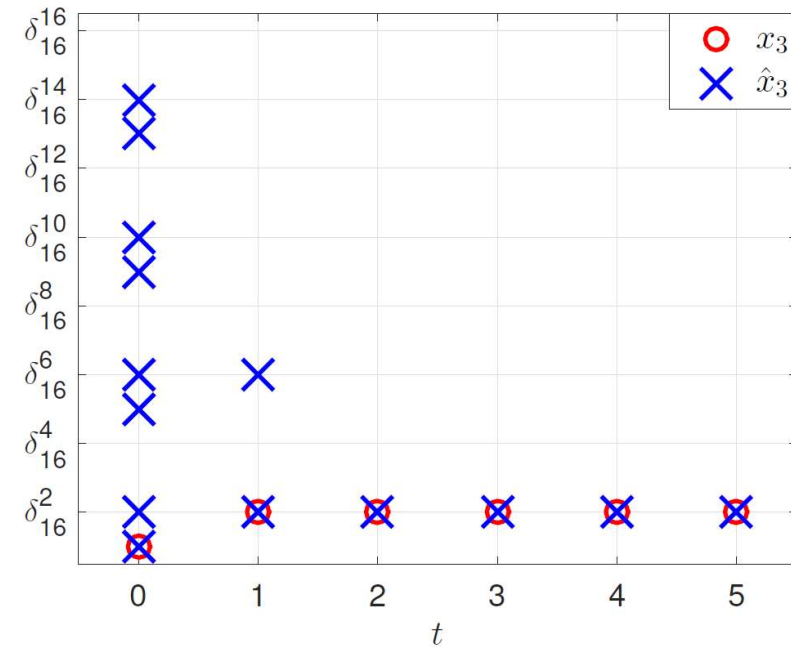
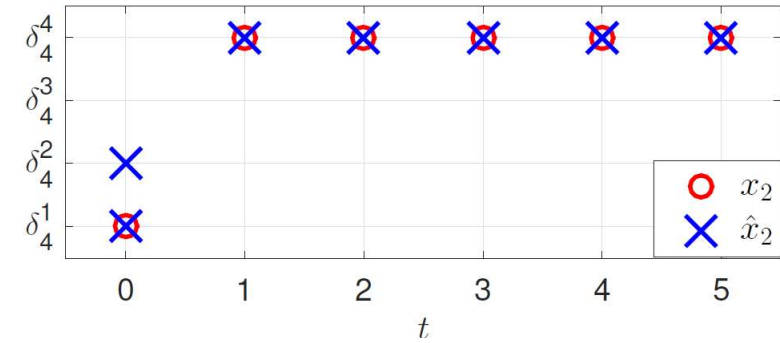
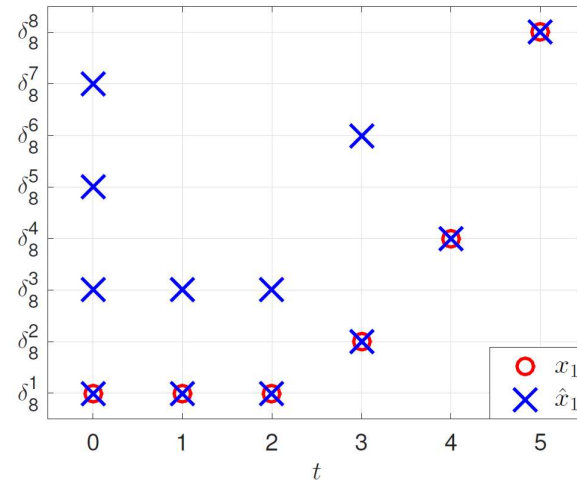
Step 3: Design a distributed observer which contains α local observers

$$\begin{aligned}\hat{x}_i(0) &= H_i^T y_i(0) \\ \hat{x}_i(t) &= \Phi_{n_i}^T(I_{2^n} \otimes H_i^T) L_i \hat{x}_i(t-1) u_i(t-1) \hat{z}_i(t-1) y_i(t) \\ i &= 1, \dots, \alpha, \hat{z}_i(t-1) \text{ are information delivered by the in-neighbors}\end{aligned}$$

Example

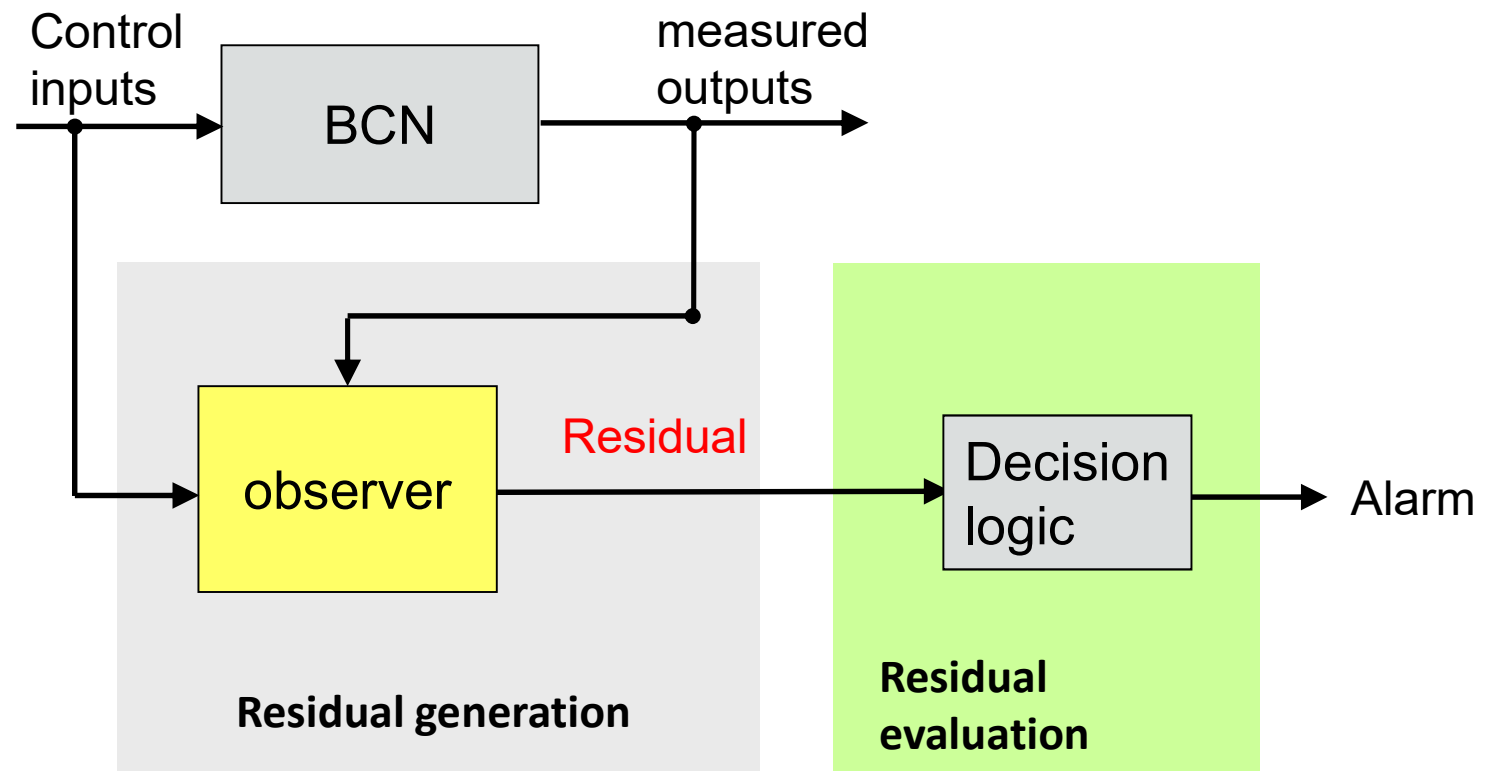
Input and output trajectory (Logical value)

t	0	1	2	3	4	5
U_1	1	1	0	0	0	
U_2	0	1	1	0	0	
Y_1	1	1	1	0	0	0
Y_2	1	0	0	0	0	0
Y_3	1	1	1	1	1	1



Fault detection of BCN

Goal: detect the abnormality in the system behaviour based on online measurement data and system model



Fault detection of BCN

Fault-free system

$$\begin{aligned}x(t+1) &= Lu(t)x(t) \\ y(t) &= Hx(t)\end{aligned}$$

Observer-based fault detector:

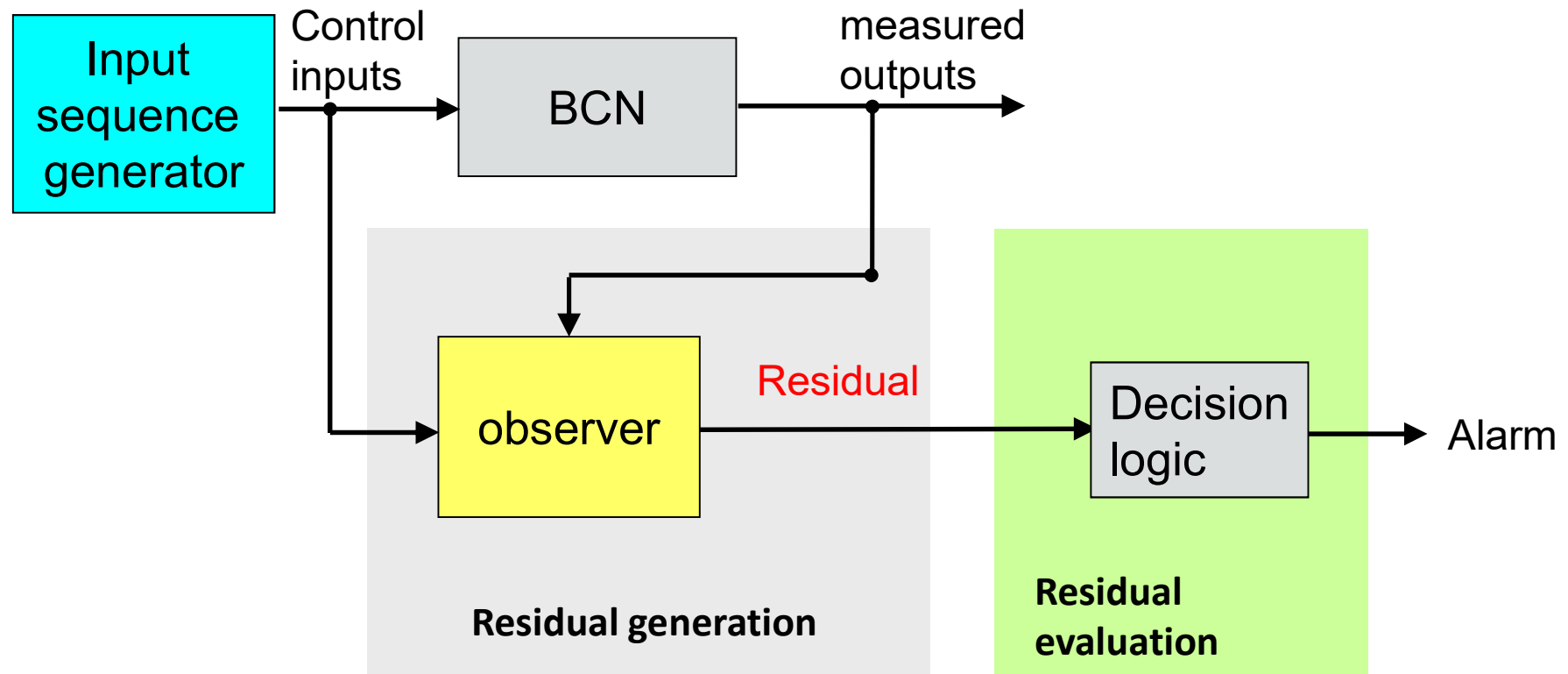
$$\begin{aligned}\hat{x}(t) &= \Phi_n^T(I_{2^n} \otimes H^T)LW_{[2^n, 2^m]}\hat{x}(t-1)u(t-1)y(t) \\ r(t) &= 1 - \mathbf{1}_{2^n}^T \hat{x}(t) \\ r(t) &: \text{residual signal}\end{aligned}$$

Decision logic:

$$\begin{cases} r(t) = 1 \\ r(t) < 1 \end{cases} \quad \begin{matrix} \Leftrightarrow \\ \Leftrightarrow \end{matrix} \quad \begin{matrix} \text{A fault has happened} \\ \text{The BCN is fault-free} \end{matrix}$$

Active fault detection

Research question: Could we design the input sequence, so that the fault better detectable?



Active fault detection

Fault-free system

$$\begin{aligned}x(t + 1) &= Lu(t)x(t) \\ y(t) &= Hx(t)\end{aligned}$$

Faulty system

$$\begin{aligned}x_F(t + 1) &= L_F u(t)x_F(t) \\ y_F(t) &= H_F x(t)\end{aligned}$$

A fault is said to be **actively detectable**, if there exists an input sequence $\{u(0), u(1), \dots, u(T)\}$, such that the output trajectories $\{y(0), y(1), \dots, y(T + 1)\}$ and $\{y_F(0), y_F(1), \dots, y_F(T + 1)\}$ generated by the fault-free system and the faulty system differ at some time instant t with $t \in [0, T + 1]$, no matter what the initial state is.

Active fault detection

Basic idea: Introduce an auxiliary state variable

$$\tilde{x}(t) = x(t)x_F(t)$$

Dynamics of the joint system

$$\begin{aligned}
 \tilde{x}(t+1) &= x(t+1)x_F(t+1) \\
 &= Lu(t)x(t)L_F u(t)x_F(t) \\
 &= L(I_{2^{m+n}} \otimes L_F)u(t)x(t)u(t)x_F(t) \\
 &= L(I_{2^{m+n}} \otimes L_F)u(t)W_{[2^m, 2^n]}u(t)x(t)x_F(t) \\
 &= L(I_{2^{m+n}} \otimes L_F)(I_{2^{m+n}} \otimes W_{[2^m, 2^n]})u(t)u(t)x(t)x_F(t) \\
 &= L(I_{2^{m+n}} \otimes L_F)(I_{2^{m+n}} \otimes W_{[2^m, 2^n]})\Phi_m u(t)x(t)x_F(t) \\
 &= \underbrace{L(I_{2^{m+n}} \otimes L_F)(I_{2^{m+n}} \otimes W_{[2^m, 2^n]})\Phi_m}_{\tilde{L}} u(t)\tilde{x}(t) \\
 &= \tilde{L}u(t)\tilde{x}(t)
 \end{aligned}$$

Active fault detection

Compare the output of the fault-free system and the faulty system

$$\begin{cases} y(t) \odot y_F(t) = 0, & \text{if } y(t) \neq y_F(t) \\ y(t) \odot y_F(t) \in \Delta_{2p}, & \text{if } y(t) = y_F(t) \end{cases}$$

Let

$$\tau = 1 - \mathbf{1}_{2p}^T (y(t) \odot y_F(t)) = \begin{cases} 1, & \text{if } y(t) \neq y_F(t) \\ 0, & \text{if } y(t) = y_F(t) \end{cases}$$

Then

$$\begin{aligned} \tau &= 1 - \mathbf{1}_{2p}^T \Phi_p^T y(t) y_F(t) \\ &= 1 - \mathbf{1}_{2p}^T \Phi_p^T H x(t) H_F x_F(t) \\ &= 1 - \mathbf{1}_{2p}^T \Phi_p^T H (I_{2n} \otimes H_F) x(t) x_F(t) \\ &= \mathbf{1}_{2^{2n}}^T x(t) x_F(t) - \mathbf{1}_{2p}^T \Phi_p^T H (I_{2n} \otimes H_F) x(t) x_F(t) \\ &= \underbrace{\left(\mathbf{1}_{2^{2n}}^T - \mathbf{1}_{2p}^T \Phi_p^T H (I_{2n} \otimes H_F) \right)}_{\tilde{H}} \tilde{x}(t) \\ &= \tilde{H} \tilde{x}(t) \end{aligned}$$

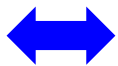
Active fault detection

The auxiliary system

$$\begin{aligned}\tilde{x}(t+1) &= \tilde{L}u(t)\tilde{x}(t) \\ \tau(t) = \tilde{H}\tilde{x}(t) &= \begin{cases} 1, & \text{if } y(t) \neq y_F(t) \\ 0, & \text{if } y(t) = y_F(t) \end{cases}\end{aligned}$$



The active fault detection problem: find an input sequence, so that $\tau = 1$, no matter what the initial state is.



An equivalent problem: Could we find an input sequence, so that the output of the auxiliary system be stabilized to 1?

Active fault detection

The equivalent problem can be solved as a deadbeat stabilization problem of autonomous switched linear discrete-time system.

Observer-based fault detector:

$$\hat{x}(t) = \Phi_n^T(I_{2^n} \otimes H^T)LW_{[2^n, 2^m]}\hat{x}(t-1)u(t-1)y(t)$$

$$r(t) = 1 - \mathbf{1}_{2^n}^T \hat{x}(t)$$

$r(t)$: residual signal

Decision logic:

$$\begin{cases} r(t) = 1 & \Leftrightarrow \text{A fault has happened} \\ r(t) < 1 & \Leftrightarrow \text{The BCN is fault-free} \end{cases}$$

Conclusion

- The STP is a useful and systematic tool that can be used to carry out observer design and fault detection in BCN
- Some algorithms can be further developed. For instance, we can find an analytical way to find the optimal partition of large-scale BCN.

Literature

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Thank you for your attention!